I. INTRODUCTION

As the efficiency and flexibility of the continuous casting process improves, it is becoming increasingly common to cast different grades of steel as successive heats in a single casting sequence. Unfortunately, mixing tends to occur during the transition between steel grades. Slabs cast during the transition vary in composition between the grade of the first heat, or "old grade" and that of the second heat, or "new grade," in the sequence. The final product is often referred to as "intermixed steel" and is naturally undesirable since it must be downgraded. The cost can be significant, since each meter of intermixed slab length contains roughly 2 tonnes of steel (for a typical 1.32 m wide slab).

The continuous casting process is illustrated in Figure 1. In this work, the term "strand" refers to the solidifying shell containing the liquid steel while it travels down through the continuous casting machine. The "slab", which is the final solid product, does not exist until the strand is completely solid and has been cut into pieces at the torch cutoff-point.

Mixing in the mold and the strand are governed by two phenomena. The first is mass transport or convection...
due to the mean flow velocities, which depends directly on the casting speed. The second is diffusion due to turbulent eddy motion and random molecular motion. Generally, the turbulent component is much more important than the molecular one due to the high turbulence in most regions of the liquid pool within the shell.

Several different ways have been developed to minimize the extent of the intermixing region during grade transitions. The most effective way is to insert a physical barrier into the mold between the two heats. Steel freezes around the steel barrier, which is often shaped like an I to help hold the two strands together. This essentially prevents any mixing of the two grades. However, this method requires the casting process to be slowed down or even stopped for a significant time, which risks damaging the strand or even the casting machine. There is also an increased risk of breakouts compared with other methods.

The most common method is simply to change ladles and carefully track and down-grade the intermixed slabs, according to the severity of the composition change due to the mixing. Sequence casting is then completely unaffected by composition changes. The disadvantage of this method is that significant mixing occurs in the tundish, in addition to the strand. Thus, several slabs containing many tonnes of intermixed steel are created.

Another common method, the "flying tundish change", is used to reduce the amount of intermixed steel generated. By changing the tundish simultaneously when changing ladles to a new grade, mixing occurs only in the strand. To accomplish the tundish change, the casting speed must always be slowed down considerably. The casting speed is then increased gradually or "ramped" back to its normal setting over several minutes, as shown in Figure 2 for an idealization of a typical practice.

The present work was undertaken to investigate mixing in the strand, focusing specifically on the latter method of grade transition. The objective is to develop and apply a mathematical model to predict quantitatively the extent of mixing in the strand and its effect on the final slab composition as a function of casting conditions. By providing insight into mixing phenomena in the continuous casting process in general, this work should also be of interest even when the tundish is not changed with every grade change.

![FIG. 2. Ramping of casting speed with time.](image)

Most of the existing work on grade transition has focused on mixing in the tundish, using both empirical methods and model calculations. Lowry and Sahaj[5] measured how the tracer concentrations evolved with time in a tundish. Burns et al[6] developed a model to evaluate the compositions at the outlet of the tundish, based on measurements of slab surface composition and liquid samples taken from the mold. Manson et al.[7] developed an empirical model to calculate the relation between the compositions and the poured steel weight in the tundish, assuming that the composition is constant in transverse cross-sections.

Mathematical models of mass transfer in the continuous casting tundish have also been developed. Tsai and Green[8] investigated this using a 3-D finite difference model. Their model was used to develop a relation between tundish transition time, tundish level (Wt%) and casting rate (Tonnes/min). In related work, tracer diffusion has been investigated with finite difference models.[9-11] None of the above-mentioned work has considered mixing in the strand.

II. 3-D MASS TRANSFER MODEL OF UPPER STRAND

Three separate finite difference models have been developed in the present work, which together enable the calculation of composition in the entire continuous casting strand and slab after a sudden grade change. The first model calculates 3-D transient turbulent fluid flow and solute diffusion in the strand. This model simulates only
the first 6 m of the strand below the meniscus. For economy, the remaining 20-40 m to the point of final solidification are modeled using a 1-D model described in the next section. Diffusion in the solid is ignored. The third model then converts the 3-D composition-time distributions from the first two models into composition-distance distributions in the final slab, according to an assumed rate of shell growth.

Figure 3 shows the 60 x 34 x 16 grid of nodes used by the first model to simulate the first 3 m of the liquid pool in the present work. A second 60 x 34 x 16 grid of nodes, which is uniform in z-direction (casting direction), was adopted from 3 m to 6 m below the meniscus. Two-fold symmetry is assumed so only one quarter of the physical strand is modeled. The effect of any gradual curvature of the strand is ignored, since it is believed to be small. The transient diffusion model calculates compositions in this 6 m domain by solving the 3-D transient diffusion equation shown in Appendix I.

To generalize the model expression for different elements, a relative concentration was introduced in this work, defined as:

$$C = \frac{F(x, y, z, t) - F_{old}}{F_{new} - F_{old}}$$  \[1\]

where $F(x, y, z, t)$ is the fraction of a given element at any specified position in the strand or slab; $F_{old}$ and $F_{new}$ are the given fractions of that element in old and new grades respectively.

A. Initial Conditions.

The fluid flow is steady state if there is no ramping or other change of the casting speed. The transient effects on the flow pattern during ramping are taken into account by a special treatment described in next section. The initial conditions on velocity are taken from the steady-state solution for the normal casting speed.

Arbitrary composition changes between successive grades can be studied through relative concentration changes of two elements, A and B. Those elements whose compositions decrease from the old grade to the new grade are represented by "element A". Elements which increase between successive heats in a sequence are represented by "element B". A constant initial condition is imposed on relative concentration:

$$t \leq 0: \quad C = \begin{cases} 1 & \text{for element } A \\ 0 & \text{for element } B \end{cases}$$  \[2\]

B. Boundary Conditions

1. Inlet:

The mold cavity is fed by a bifurcated, submerged entry nozzle, which has an important influence on the flow pattern. To account for this, velocity components and turbulence parameters are fixed at the inlet plane to the mold cavity. The inlet dimensions, $L_b$ and $L_{wp}$, correspond to the area of the nozzle port where steel flows outward. Because a relative stagnant region exists in the top portion of typical oversized ports of nozzles used in service,\[12,13\]$L_b$ is shorter than the actual height of the nozzle port, given in Table I and correspond to conditions at the exit plane from the nozzle port. They are calculated using a separate model of fluid flow in the nozzle, described elsewhere.\[12,13\]
Relative concentration of element A simply decreases suddenly from 1 to 0 across the inlet plane (nozzle exit) at the time instance when the transition starts. The inlet concentration is kept at this value 0 afterwards. This corresponds to a "flying-tundish change" operation. Relative concentration of element B is the reverse of A:

\[ t > 0 : \quad C_0 = \begin{cases} 
0 & \text{for element A} \\
1 & \text{for element B} 
\end{cases} \quad [3] \]

### 2. Outlet, Symmetry Planes, and Top Surface.

Because calculations are performed with the 3-D model only in the top portion of the liquid pool, an artificial outlet plane is created where flow leaves the domain. Across this bottom outlet plane, normal gradients \((\partial \phi/\partial z)\) of all variables are set to zero. The same boundary conditions are used for each node on a symmetry centerplane, except

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Variable</th>
</tr>
</thead>
<tbody>
<tr>
<td>a\textsubscript{1}, a\textsubscript{2}, a\textsubscript{3}</td>
<td>Empirical constant in Eq.[4]</td>
</tr>
<tr>
<td>C</td>
<td>Relative concentration in the strand</td>
</tr>
<tr>
<td>C\textsubscript{0}</td>
<td>Relative concentration at inlet (for 3-D modeling)</td>
</tr>
<tr>
<td>D\textsubscript{eff}</td>
<td>Effective diffusivity</td>
</tr>
<tr>
<td>D\textsubscript{0}</td>
<td>Molecular diffusivity</td>
</tr>
<tr>
<td>F</td>
<td>Fraction of a given element</td>
</tr>
<tr>
<td>L\textsubscript{h}</td>
<td>Inlet height</td>
</tr>
<tr>
<td>L\textsubscript{w}</td>
<td>Inlet width</td>
</tr>
<tr>
<td>L\textsubscript{m}</td>
<td>Working mold length</td>
</tr>
<tr>
<td>L\textsubscript{n}</td>
<td>Nozzle submergence depth</td>
</tr>
<tr>
<td>N</td>
<td>Slab mold thickness (across narrow face)</td>
</tr>
<tr>
<td>Re</td>
<td>Reynolds number</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>Sc\textsubscript{t}</td>
<td>Turbulent Schmidt Number</td>
</tr>
<tr>
<td>t</td>
<td>Time</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>v\textsubscript{c}</td>
<td>Casting speed</td>
</tr>
<tr>
<td>v\textsubscript{r}\textsubscript{min}</td>
<td>Minimum casting speed during ramping</td>
</tr>
<tr>
<td>W</td>
<td>Slab mold width</td>
</tr>
<tr>
<td>Z\textsubscript{final}</td>
<td>Metallurgical Length</td>
</tr>
<tr>
<td>Z\textsubscript{1}</td>
<td>Strand length simulated by 3-D model, where switching from 3-D model to 1-D model</td>
</tr>
<tr>
<td>z</td>
<td>Distance from transition point (casting direction)</td>
</tr>
<tr>
<td>(\alpha)</td>
<td>Inlet jet angle</td>
</tr>
<tr>
<td>(\mu\textsubscript{eff})</td>
<td>Effective viscosity (liquid steel at inlet)</td>
</tr>
<tr>
<td>(\mu_0)</td>
<td>Laminar (molecular) viscosity</td>
</tr>
<tr>
<td>(\mu_t)</td>
<td>Turbulent viscosity (liquid steel at inlet)</td>
</tr>
<tr>
<td>(\rho)</td>
<td>Density (liquid steel)</td>
</tr>
</tbody>
</table>

\textsuperscript{†} Based on typical 15° down 90x60 mm rectangular nozzle.\textsuperscript{13}
that the velocity component normal to the symmetry plane is set to zero. The top surface is treated as a symmetry plane.

Zero-gradient or "no mass diffusion" boundary conditions were imposed on relative concentration at the outlet plane, the symmetry planes and the top surface.

3. Other Boundaries

Because the model domain is the entire strand, zero-gradient or "no mass diffusion" boundary conditions were also imposed at the other boundaries, which correspond to the strand surface. This prevents solute from leaving the domain at these boundaries. For computational convenience, the models simulate both the solid and liquid, using liquid properties everywhere. However, the error inherent in this approximation is not significant because results calculated in the solid are never used in the subsequent slab calculations (to predict slab composition).

C. Ramping of Casting Speed

To account for the effect of ramping the casting speed on the flow pattern, without incurring huge expenses in modeling 3-D transient turbulent fluid flow, a compromise approach is utilized in the present work. At each time step, the steady-state velocity solution was scaled uniformly by the ratio of the current inlet velocity to the steady-state value. This approach relies on two reasonable assumptions. Firstly, the steady-state flow pattern (streamlines) does not vary with speed or Reynolds number when the flow is fully turbulent.\(^{[14]}\) Secondly, the transient pressure wave moves at the acoustic speed,\(^{[15]}\) so should propagate the effect of the new inlet velocities throughout the mold almost immediately. The casting speed curve used in the present work is shown in Figure 2, which approximates that used in practice.\(^{[2]}\)

D. Solution method

1. Fluid Flow Velocities

Owing to the regular rectangular geometry of the mold, a computer code based on finite difference calculations, MUPFAHT\(^{[16]}\) has been chosen to solve the steady-state (elliptic) system of differential equations and boundary conditions, which describe this problem. The finite difference equations use a staggered grid and seven-point stencil of control volumes, discretized spatially using a hybrid scheme which generally has second-order accuracy but automatically switches to a first-order upwinding scheme in domains with high cell Reynolds number.\(^{[17]}\) In addition, the source terms are linearized to increase diagonal dominance of the coefficient matrix.\(^{[17]}\)

The equations are solved with the Semi-Implicit Method of Pressure-Linked Equations algorithm, whose ADI (Alternating-Direction-semi-Implicit) iteration scheme consists of 3 successive TDMA (Tri-Diagonal-Matrix Algorithm) solutions (one for each coordinate direction) followed by a pressure-velocity-modification to satisfy the mass conservation equation.\(^{[17]}\)

Obtaining reasonably-converged velocity and turbulence fields for this problem is difficult, owing to the high degree of recirculation. The current strategy employed is successive iteration using an under-relaxation factor of 0.2 or 0.3 until the maximum relative residual error and maximum relative error between successive solutions falls below 0.1 pct. Over 2500 iterations are required to achieve this, starting from an initial guess of zero velocity, which takes about 30 CPU hours on an SGI (Silicon Graphics 4D/25 workstation). For subsequent processing conditions, convergence from a previously-obtained solution is faster.

2. Mass Transfer

The 3-D transient diffusion equation is solved after the velocity solution has been obtained, since it can be uncoupled. This solution is obtained using the backward Eulerian method, which is a fully implicit scheme for time discretization. Variable time step increments were taken to assure a relative time truncation error of 0.1 p. Within each time step, usually several hundred ADI TDMA iterations are needed to reach convergence. A simulation of 960 s of casting requires about 50 time steps and 8 hours of CPU time on the SGI.

III. 1-D MASS TRANSFER MODEL OF LOWER STRAND

The point of final solidification, the "metallurgical length", is found about 20 m from the meniscus, or further depending on the casting speed. The slab center takes about 20 minutes to reach this point at the casting speed of 1 m/min. Therefore, composition evolution for this time
period must be calculated over this entire domain of the strand before it is possible to predict the complete composition distribution in the final slabs. A huge number of grid nodes would be needed for the 3-D model to obtain reasonable results. On the other hand, the initial 3-D results for the top 6 m show that the velocity profile in the lower region of the strand is quite uniform and close to that of turbulent flow through a duct. Furthermore, the composition profile is almost uniform in the transverse section. Based on this knowledge, a 1-D mass transfer model was developed and applied below the point, Z₁, usually chosen to be 6 m down the strand. The inlet boundary conditions are specified from 3-D model predictions of the velocity and concentration distributions at the outlet of the upper domain (Z₁=6 m below the meniscus).

The model equations were solved with the same time integration and spatial difference schemes used for the 3-D model. It took only about 2 minutes CPU time on the SGI, with an 800 node mesh of a 14 m long domain.

Because of its computational efficiency, the 1-D model was later extended to evaluate the entire composition history along the centerline from the meniscus without use of 3-D results for the upper 6 m. For these runs, the turbulent diffusivity was enhanced 15 times in top 3 m of the strand to account for the effects of 3-D flow. The velocity solution became the casting speed, which depends only on time because of ramping. The inlet boundary was put right at the meniscus and the relative concentration at this boundary was switched from 1 to 0 for element A and from 0 to 1 for element B when the transition starts.

IV. SLAB COMPOSITION MODEL

The distribution of compositions in the final slab develops as the solidifying shell grows in thickness down the caster. The third model of this work calculates these composition distributions in the final slab based on the 3-D, time-varying concentration history of the strand, generated by the first two models. Composition at each point in the strand is assumed to evolve according to the calculated history until that point solidifies. The composition is assumed to remain constant thereafter, so that diffusion in the solid is ignored.

Mathematically, this model performs a coordinate transformation on the strand results to obtain the composition in the final slab. To do this, a shell growth rate, which depends on spray cooling conditions at the strand surface, was chosen from among the typical values reported from previous measurements in the strand. It should noted that the model neglects any delays in the adjustment of the shell thickness to reach the new steady-state profile after a sudden change in casting speed. This might have a small effect at the beginning of ramping.

V. MODEL RESULTS

Model calculations of velocity, composition in the strand and in the slab are now presented and compared with available measurements. The results were obtained by running the standard combination of three models, i.e. 3-D model for the top 6 m, 1-D model for the rest of the strand, and slab composition model, all under standard casting conditions shown in Table I, except where otherwise indicated.

A. Flow Pattern

Figure 4 presents typical velocity predictions in the top 3 m portion of the strand. This figure views the centerline section and shows how flow leaves the nozzle as a strong jet, traveling across the mold to impinge upon the narrow face, then splitting vertically to create upper and lower recirculation regions. This turbulent flow pattern enhances the transport of mass, momentum and energy in the upper region of the strand. The figure also shows that velocity is quite uniform in the downstream region, 2.5 to 3 m below the meniscus. In the lower portion of the strand, steel moves vertically in the casting direction. By 6 m below the meniscus, the velocity solution closely approximates 1-D channel flow with an average velocity equal to the casting speed.

B. Strand Composition

The relative concentration distribution calculated in the first 6 m portion of 1/4 of the strand is revealed in Figure 5 at different time steps. This figure depicts the evolution of relative concentration of element B, which equals the fraction of new grade present. The isoconcentration contours shown in this figure outline the spread of element B due to the combined effects of convection and diffusion.
The jet brings steel containing 100% relative concentration element B into the strand at the inlet. As the jet moves, it carries element B with it. Where the jet impinges the narrow face, it carries mass both upwards and downwards. At the same time, the strong turbulence causes mass diffusion in all directions. In the upper region, the narrow face shell sees the new steel grade first so that always has highest concentration of element B at any time. Combined with the upper recirculation zone, the upper portion of the mold very quickly approaches the composition of the new grade (rich in element B). At the meniscus, where the first solidification takes place and the composition of the slab surface is determined, the narrow surface has a slightly higher concentration of element B than the centerline of the strand, producing a slight concentration gradient across the mold width direction on the wide surface of the strand. This effect diminishes with time. Relative concentration across the meniscus is more than 95% B after 480 s.

In the lower region of the strand, the isoconcentration lines in Figure 5 show behavior corresponding to the uniform velocity solution. They shift downward with time and become more uniform across the strand. Due to diffusion, they move slightly faster than the casting speed. The extra mean velocity due to this diffusion effect adds to the bulk average movement of steel and is called the "diffusion velocity". This diffusion velocity decreases as the concentration gradients reduce over time. As time increases, the strand eventually becomes filled with the new grade, as indicated by the general increase in B concentration with time.

![Graph showing concentration in strand](image)

**FIG. 4.** Predicted flow pattern in first 3m portion of strand.

![Graph showing concentration in strand](image)

**FIG. 5.** Relative concentration of element B in strand.

Figure 6 presents the concentration history of a particular point in the strand (6 m below the meniscus at the centerline). The relative concentration of element B stays at zero for 100-250 seconds, indicating a significant component of plug flow through the strand. Relative concentration then increases rapidly, before slowing down to gradually approach 100% (the new grade). This effect indicates the diffusion backmixing component of the flow.
Figure 6 also shows the effect of "ramping" the casting speed according to Figure 2. The lower average velocity of steel in the strand increases the time to reach a given concentration. The curve predicted with ramping shows a time lag of about 120 s behind that predicted without ramping. This corresponds to the time difference between bulk movement in the two cases.

C. Slab Composition

Based on the predicted composition histories in the strand, the final composition distribution in the slab was calculated and investigated under the conditions in Table I. Figure 7 presents the isoconcentration contours on the surface of a quarter slab with a length of 12 m and Figure 8 shows corresponding results in transverse sections through the interior. Together, these figures show the dramatic differences in composition that arise both down the slab and between the slab surface and interior.

![Figure 6](image6.png)

**FIG. 6.** History of relative concentration of element B (at center line of strand, 6 m below meniscus).

![Figure 7](image7.png)

**FIG. 7.** Relative concentration of element B at slab surface.

![Figure 8](image8.png)

**FIG. 8.** Relative concentration of element B inside slab.

The slab surface, which is created at the meniscus, has relatively straight isoconcentration lines across the slab width. Before the transition, the surface composition is naturally 100% of the old grade, containing 0.0 B. The composition then sharply changes at the "transition point", which corresponds to the part of the slab that was solidifying at the meniscus at the time the grade change began. This transition point is consistent with the "double pour point," which refers to the lines formed on the surface of the slab due to the casting speed changes. The transition point defines the origin (0) in the z casting direction of the slab. The fraction of new grade increases rapidly after (above) this point and reaches 95% at the wide face surface by -6 m position in the figure.

It is interesting to notice the slightly (3% - 10%) higher composition at the narrow face than at the center of wide face near the transition point. This variation across the mold width is produced because the meniscus at the narrow face wall always meets new steel coming from the nozzle before the center line.

Mixing in the strand is very important to composition in the slab interior. Figures 7 and 8 show that the new grade reaches about 10% near the wide face center plane at 6 m below the transition point. This illustrates how deeply new grade penetrates into the slab. Combined with mixing at the surface, a total of about 14 m of intermixed slab is produced, based on an mixing criterion of between 5% and 95% new or old grades. The intermixing length at the center is about 10 m using the same criterion, while the corresponding length along the surface is only 6 m.
Comparing Figure 8 with Figure 5 shows how the combined effects of solidification and mixing make the composition developed in the slab very different from the distributions calculated in the strand. As the strand moves during casting, the composition becomes fixed upon solidification at the shell interface. The resulting isoconcentration lines in the slab are almost all parallel to the mold walls, perpendicular to the direction of growth of the columnar dendrites. At 6 m below the transition point, this composition distribution affects only the center region and might be mistaken for centerline segregation.

Figure 8 also predicts some interesting reversals in concentration gradient moving into the slab. These are due to solidification of regions where the fluid is moving upward in the opposite direction of the casting speed. The magnitude of the effect is not particularly significant.

These figures show that intermixing is not uniform within the slab. The surface is intermixed only above the transition point. In contrast, the center line has much deeper intermixing below. This effect is seen more clearly in Figure 9, which presents the relative concentration of element B down the slab at different depths beneath the surface. The surface longitudinal composition gradient is largest near the transition point and is generally greater than the gradients inside the slab. The concentration curves show long tails extending above the transition point at the surface and below the transition point at the center. The furthest extent of intermixing is found at the center of the slab below the transition point.

Based on Figure 9, the length of the intermixing region could be defined in several different ways, according to the mixing criterion and whether surface or interior is more important. Estimation of the intermixing length based solely on surface composition measurements would ignore a significant intermixing length in the center below the transition point.

The intermix length could alternatively be based on the average composition across the transverse section, which is presented in Figure 10. These results are naturally intermediate between those of the surface and centerline. The average intermixing distance is thereby shorter than that based on local compositions (Figure 9). It is shortened the most below the transition point because the slab is completely old grade in this region, except at the center.

VI. MODEL VERIFICATION

A. Comparison between 1-D and 3-D Strand Models

The results predicted by the simple 1-D model are compared with those of the 3-D model in several ways. Relative concentration results in the strand are compared for the region of 3 m to 6 m in Figure 6. The velocity and concentration inlet conditions at 3 m plane were taken from a separate 3-D model run in both cases. It is seen that good agreement between both models has been achieved, indicating that 1-D diffusion (complete mixing across slab lateral sections) is a reasonable assumption after 3 m. The greatest deviation occurs in the initial period when the concentration first increases above zero. The 1-D model slightly underestimates mass transport at this time and correspondingly overestimates it later. These results imply that the 1-D model should be adequate lower in the strand (below 6 m) where this assumption is even more reasonable.
In Figure 9, the 1-D model was run starting from the meniscus with a 15 times enhancement of diffusivity for the first 3 m top portion of the strand to account for the effect of 3-D flow and mixing. This extended 1-D model predicts the same concentrations in the slab centerline as the 3-D model. The 1-D model assumes a sudden jump from 0 to 1 at the transition point at the slab surface so is less accurate at predicting composition closer to the surface. This is also reflected in the crude prediction of average composition, which is indicated in Figure 10.

B. Comparison between Strand Model and Analytical Solution

The upwinding scheme used to develop the finite difference equations is known to cause potential numerical problems called "numerical diffusion" and "numerical dispersion." The latter problem is related to flow that is not parallel to any of the coordinate axes. Because flow in the strand is predominantly parallel to the casting direction, which is aligned with the z axis, attention was focused on the extent of false numerical diffusion in this direction.

To verify the accuracy of the transient mass transfer models in the strand and to investigate the influence of numerical diffusion, a 1-D analytical solution was found for the special case of no diffusion, simply by transforming a constant concentration profile from a Lagrangian system to the present Eulerian system.

A solution was obtained on a 16.6 m long domain starting from Z1 (3 m) down the strand under conditions in Table I with constant casting speed. The inlet condition at Z1 was taken from time-dependent results from the 3-D model, as described before. The results are compared in Figure 11 with the predictions of the 1-D mass transfer model, run under the same conditions both with and without turbulent diffusion. The discrepancy between the analytical solution and the model run without diffusion is attributed to false numerical diffusion.

The results show that numerical diffusion in the casting direction below 3 m in the strand is much smaller than turbulent diffusion and has very small effect on the prediction. The greatest error arises in the initial stages of mixing, where the maximum effect of numerical diffusion reaches 30% of the turbulent diffusion results.

![Figure 11 - Effect of numerical and turbulent diffusion on concentration histories at specified points along strand.]

These results indicate that turbulent eddy motion in the liquid pool greatly enhances mass transport, as it does transport of momentum and energy as well.

C. Comparison between Slab Composition Predictions and Measurements

The slab model predictions of relative concentration down the slab centerline are compared in Figures 12 and 13 with the measurements from Gas et al. of Inland Steel. The predicted compositions were determined using all three models, as described in sections II-IV. Casting conditions for both measurements and predictions are given in Table I. Overall agreement is good, as the same trends for both the predictions and the measurements can be seen in the figures.

Any real difference in mixing behavior between different elements is due to differences in their molecular diffusivities in liquid steel, which are shown in Table III to range from $5 \times 10^{-9}$ to $5 \times 10^{-7} \text{ m}^2/\text{s}$. These values are at least three orders of magnitude smaller than the turbulent diffusivity of $6.7 \times 10^{-4} \text{ m}^2/\text{s}$ calculated with the data in Table I assuming the turbulent Schmidt number to be 1. Thus, diffusion is dominated by the turbulent component of diffusivity. Differences in the molecular diffusivities have almost no effect on diffusion.

Mixing behavior is controlled by mass convection, through the flow pattern, and turbulent mass diffusion. This is consistent with previous findings that momentum and heat transfer in the continuous caster are dominated by the turbulent viscosity and turbulent conductivity respectively. Since different elements should be affected equally by turbulence, no difference is predicted between the relative concentrations of different elements in


to affect only the liquid properties: density, viscosity, and diffusivity. Density changes are very small (< 0.1%). Other variables have almost no effect on the results because only changes in the laminar properties were investigated. Turbulence dominates both the flow (through the turbulent viscosity) and the mass transfer (through the turbulent diffusivity). Thus, changes of more than a factor of 4 in the molecular viscosity and one or two orders of magnitude in the molecular diffusivity have no observable effect on either the flow or the mass transfer. Further studies were not conducted because the turbulent properties of liquid metals are not known well enough to properly modify the parameters concerned with turbulence properties. It is strongly suspected that the effect of element type is always negligible, so all elements intermix about the same, as discussed before. The only possible exception is carbon, whose rapid diffusion in the solid state may make a slight difference that has been ignored in this work.

To minimize the intermixed steel generated, the results presented in this work could be used in conjunction with a grade-dependent criterion to determine the length of steel to be downgraded for the given casting conditions. The torch cut-off could be programmed to cut off exactly this length of slab for downgrading.

Gravity segregation due to density differences has been ignored in this work. It is a complicated and open problem in mixing research in the continuous casting processes.

B. Mold Width

The model was next run to investigate the effect of mold width on mixing in the strand and slab. To maintain the same casting speed, the flow rate through the nozzle is lower into narrow slabs. The resulting lower velocities decrease turbulence in the mold cavity, which tends to reduce diffusion in the strand. Figure 14 compares the concentration along the slab centerline for different mold widths. The lower diffusivity in the narrow mold results in a slightly sharper concentration change, but the difference is very small. Thus, mold width has no significant effect on mass transfer and mixing behavior. The effect of mold width is much more important when there is mixing in the tundish. In this case, wider molds exhibit shorter intermixing lengths, since the same amount of mixed liquid from the tundish is cast as a shorter slab. [6]
### TABLE II: CASTING CONDITIONS IN PLANT[2]

<table>
<thead>
<tr>
<th>Trial</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mold Width (m)</td>
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<td>0.986</td>
<td>0.842</td>
<td></td>
</tr>
<tr>
<td>Minimum Casing Speed $V_{\text{cmin}}$ (m/min)</td>
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<td>0.2</td>
<td>0.2</td>
<td>0.2</td>
</tr>
<tr>
<td>Normal Casting Speed $V_{\text{c}}$ (m/min)</td>
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<td>Ramping Time (min)</td>
<td>3.5</td>
<td>4</td>
<td>4.8</td>
<td>4.8</td>
</tr>
<tr>
<td>Distance Traveled during ramping (m)</td>
<td>2.077</td>
<td>2.378</td>
<td>2.925</td>
<td>2.909</td>
</tr>
</tbody>
</table>

### TABLE III: MOLECULAR DIFFUSIVITY[18, 19]

<table>
<thead>
<tr>
<th>Element</th>
<th>Diffusivity ($m^2/s$)</th>
<th>Conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mn</td>
<td>$4.6 \times 10^{-7}$</td>
<td>0 - 10 %, 1550 - 1700 °C</td>
</tr>
<tr>
<td></td>
<td>$4.37 \times 10^{-9}$</td>
<td>0 - 5.4 %, 1550 °C</td>
</tr>
<tr>
<td>Si</td>
<td>$5.1 \times 10^{-8}$</td>
<td>0 - 4.4 %, 1550 - 1725 °C</td>
</tr>
<tr>
<td></td>
<td>$7.9 \times 10^{-9}$</td>
<td>0.03 %, 1550 °C</td>
</tr>
<tr>
<td>C</td>
<td>$5.9 \times 10^{-9}$</td>
<td>2.1 %, 1550 °C</td>
</tr>
<tr>
<td></td>
<td>$4.3 \times 10^{-8}$</td>
<td>2.5 % in Fe-C, 1500 °C</td>
</tr>
<tr>
<td></td>
<td>$4.4 \times 10^{-7}$</td>
<td>0.05 % in Fe-C, 1564 °C</td>
</tr>
</tbody>
</table>

**C. Ramping of Casting Speed**

Slowing down and gradually speeding up the casting speed during a grade change has a significant effect on both mixing in the strand and solidification. The overall slower casting speed involved with ramping increases the time needed to reach a given concentration in the strand, as described in section V and Figure 6. This tends to reduce the extent of intermixing in the slab. At the same time, however, the slower speed of the shell also decreases the metallurgical length. This almost compensates for the previous effect. The net effect of ramping the casting speed is to slightly shorten the intermixing length, as shown in Figure 15. The longer the ramping time, (i.e. slower ramping speed), the shorter the intermixing length.

**D. Casting Speed**

Casting speed has little qualitative effect on flow pattern in the strand. The magnitudes of the velocities simply change proportionally. However, the casting speed has a significant effect on both mixing in the strand and solidification.

Similar to the effect of ramping, the influence of the concentration increase in the strand due to the increase of the casting speed is partly canceled by the increase of solidification length (metallurgical length). Thus, the effect of the casting speed on concentration in the strand is much greater than its effect on slab composition. The extended 1-D model was run with four different casting...
speeds to investigate this important casting variable. Inlet conditions varied with the casting speed according to the previous separate model predictions, using a separate model of the nozzle\textsuperscript{[13]} and are listed in Table IV.

The results in Figure 16 confirm that increasing casting speed increases the intermixing length. The larger the casting speed, the longer the intermixing length.

From the model results, an empirical equation was fit to reproduce relative concentration down the centerline of the slab as a function of the casting speed:

$$C = C_0 \cdot \frac{C_0}{2} \cdot \text{erf} \left( \frac{a_1 + a_2 z}{a_3} \right) \exp \left( -\frac{Vc}{a_3} \right)$$ \hspace{1cm} [4]

$$C_0 = 1, \; a_1 = -1.2, \; a_2 = 0.4, \; a_3 = 0.0333$$

The results produced from Equation [4] are also included in Figure 16. This model might be modified to account for time variation in $C_0$ due to mixing in the tundish.

<table>
<thead>
<tr>
<th>Casting Speed (m/min)</th>
<th>Turbulent Kinetic Energy K (m$^2$/s$^2$)</th>
<th>Dissipation Rate $\epsilon$ (m$^2$/s$^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.0212</td>
<td>0.0839</td>
</tr>
<tr>
<td>1.0</td>
<td>0.0502</td>
<td>0.3935</td>
</tr>
<tr>
<td>1.5</td>
<td>0.0850</td>
<td>1.0920</td>
</tr>
<tr>
<td>2.0</td>
<td>0.1282</td>
<td>2.2932</td>
</tr>
</tbody>
</table>

VIII. CONCLUSIONS

1. A mathematical model has been developed to calculate the mixing in the strand and the slab during steel grade transition in the continuous slab casting process, based on turbulent 3-D fluid flow and mass transfer. The model calculations show good agreement with available experimental measurements for a simultaneous grade change and flying tundish change.

2. Mixing in the strand is significant, affecting more than 25 tonnes of steel and creating 14 m of intermixed slab under typical casting conditions (Table I) for an intermixing criterion of 5% - 95%. This is important, regardless of whether the tundish is changed at the time of the grade change or not.

3. The intermixing length depends mainly on the mold thickness and is not affected by the mold width for the conditions studied.

4. Significant increase of the casting speed produces slightly more intermixing in the slab. Higher speeds decrease the time needed to reach a given concentration in the strand. This is partially compensated by the simultaneous increase in the metallurgical length. Ramping the casting speed also has a slight effect on intermixing in the slab through its slowing down of the average casting speed.

5. Different elements were found to have the same mixing behavior under the same casting conditions, despite having different molecular properties. This is because the mass transport of solute due to turbulent eddy motion is many orders of magnitude bigger than molecular diffusions and thus dominates the resulting composition distributions.
6. Numerical diffusion caused by finite difference schemes was confirmed to be much less important than turbulent diffusion. In the lower portion of the strand (e.g., 3 meters below the meniscus), the flow and diffusion can be reasonably approximated as 1-D.

**APPENDIX I  MASS TRANSFER MODEL IN STRAND**

3-D transient diffusion equation:

\[
\frac{\partial C}{\partial t} + v_x \frac{\partial C}{\partial x} + v_y \frac{\partial C}{\partial y} + v_z \frac{\partial C}{\partial z} = \frac{\partial}{\partial x} \left( D_{eff} \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left( D_{eff} \frac{\partial C}{\partial y} \right) + \frac{\partial}{\partial z} \left( D_{eff} \frac{\partial C}{\partial z} \right)
\]

[A-1]

To calculate the velocities \( v_x, v_y \) and \( v_z \) needed in the above equation, a 3-D fluid flow model was used, including the continuity, 3 momentum and 2 turbulence equations given in Appendix I. Further discussion of how this fluid flow model works and comparisons of the model results with water model observations and measurements are given elsewhere.\(^{[12, 13]}\)

The Reynolds number in the caster, based on the hydraulic diameter, (Table I) always exceeds 10,000 even far below the mold. This indicates that the flow is highly turbulent everywhere. Thus, the K-\( \varepsilon \) turbulence model is used in calculating velocities.\(^{[13]}\) In addition, diffusion is enhanced greatly by turbulent eddy motion, so the effective diffusivity, \( D_{eff} \), consists of both molecular and turbulent components:

\[
D_{eff} = D_0 + \frac{\mu_t}{\rho S_{Sc}}
\]

[A-2]

The effective diffusivity depends greatly on the turbulence parameters through the calculated turbulent viscosity, \( \mu_t \), and the turbulent Schmidt number, \( S_{Sc} \), which is set to 1 \(^{[10, 11, 20, 21]}\).

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**REFERENCES**


